

# Calculation of miniband structure in strain-balanced type-II GaAsBi/GaAsN superlattice

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# Outline

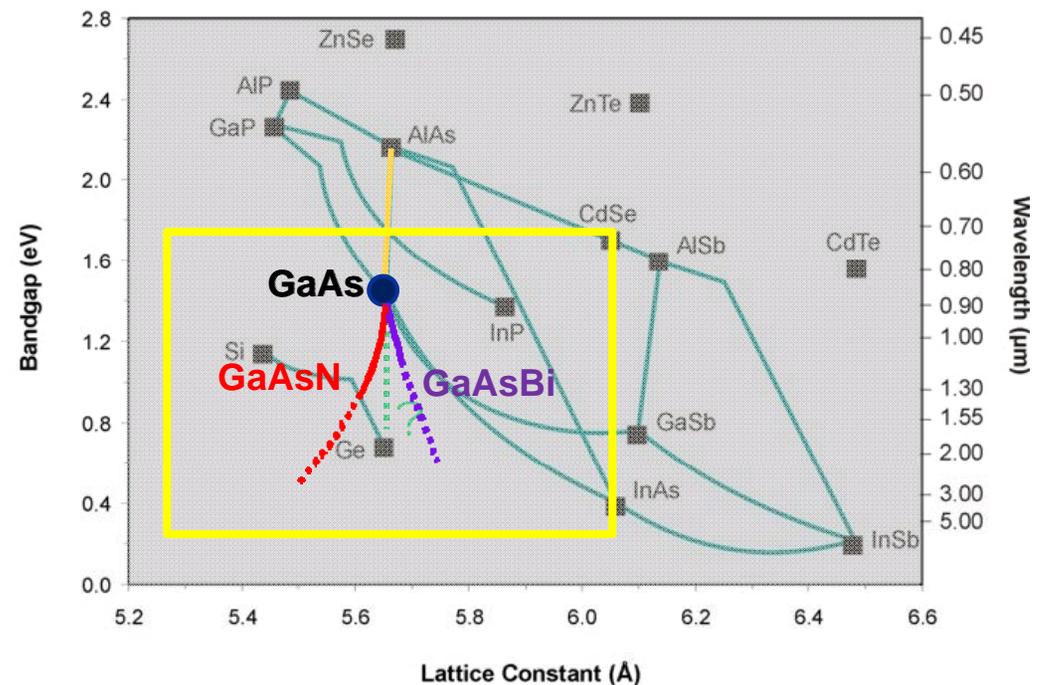
- **Motivations for GaAsBi/GaAsN Type-II SLS**
- **Study Objectives**
- **Calculation Methodology**
  - ▣ Strain-Balanced Criteria
  - ▣ Band alignment and Strain effect
  - ▣ Schrödinger – Poisson Self-Consistent Equation
- **Results**
- **Future work**
- **Conclusion**





# Motivations for GaAsBi/GaAsN

- **Desire narrow bandgap material with effective lattice match to GaAs**
  - Key for low-cost GaAs technology
  - Particularly important for optoelectronic devices such as detectors where thick active regions required
  - Lasers
  - Photodetectors
  - Solar Cells





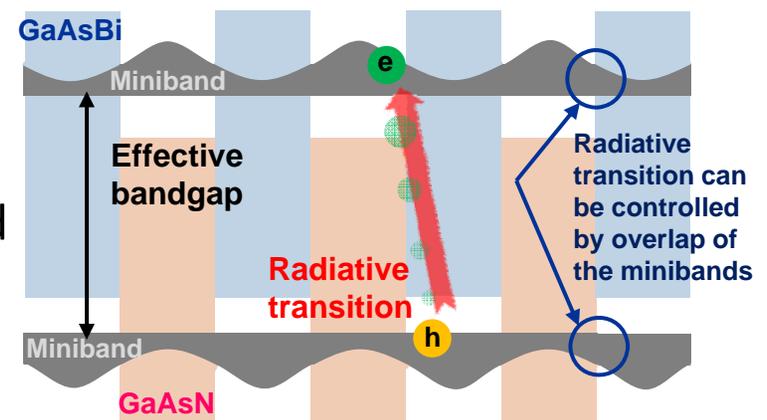
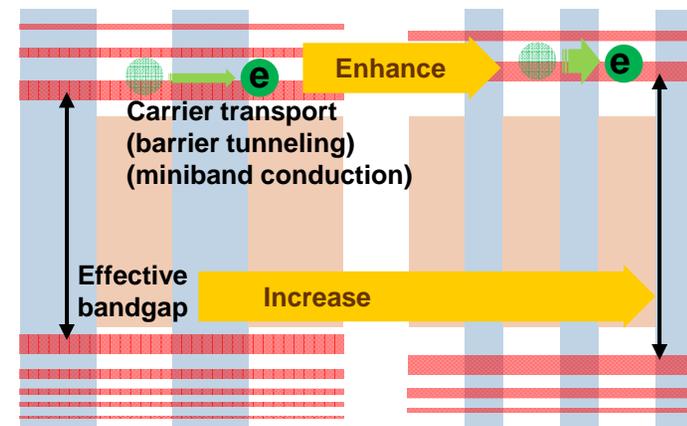
# Motivations for Type-II SLS

## Advantages of superlattices – Bandstructure engineering

- Effective bandgap
- Electronic transport
- Controlled by layer thickness

## Advantages of GaAsBi/GaAsN Type-II superlattice

- Effective lattice match to GaAs
- Minibands in conduction/valence band can be independently controlled
- Radiative transitions (lifetime, absorption) can be controlled





# Study Objectives

- **Develop method for calculating electronic structure**
  
- **Determine range of transition energies for SLS**
  - ▣ Strain balanced structures
  - ▣ “Reasonable” Bi and N content (up to 5% Bi and N composition)
  - ▣ Varying thickness for GaAsBi, GaAsN layers
  
- **Initial objective to determine criteria to achieve “1 eV” material for photovoltaics**





# Simulation Methodology

## 1 Strain-balanced Criteria

- Determine precondition of concentrations of Bi and N using the strain-balanced criteria on a GaAs substrate

## 2 Band alignment of GaAsBi/GaAsN superlattice

- Obtain band edge discontinuity of the heterostructure based on GaAsBi and GaAsN band alignment
- Consider strain effect due to lattice mismatch

## 3 Miniband calculation using Schrödinger – Poisson equation

- Simulate energy states in the superlattice using self consistent Schrödinger – Poisson equation
- Transfer matrix algorithm used to solve Schrödinger equation

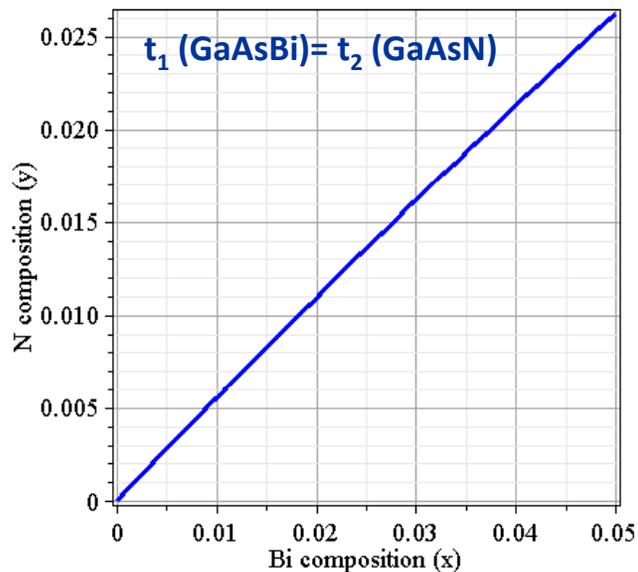




# Strain-Balanced SLS

## □ Strain - balanced criteria on GaAs substrate

- Balancing compressive strain (GaAsBi) and tensile strain (GaAsN)
- Condition of zero average in-plane stress<sup>[1]</sup>



$$\frac{\partial U_{av}}{\partial \epsilon_1} = \frac{2}{t_1 + t_2} \left( t_1 A_1 \epsilon_1 + t_2 A_2 \epsilon_2 \frac{a_1}{a_2} \right) = 0$$

Results: GaAs<sub>1-x</sub>Bi<sub>x</sub> / GaAs<sub>1-y</sub>N<sub>y</sub>

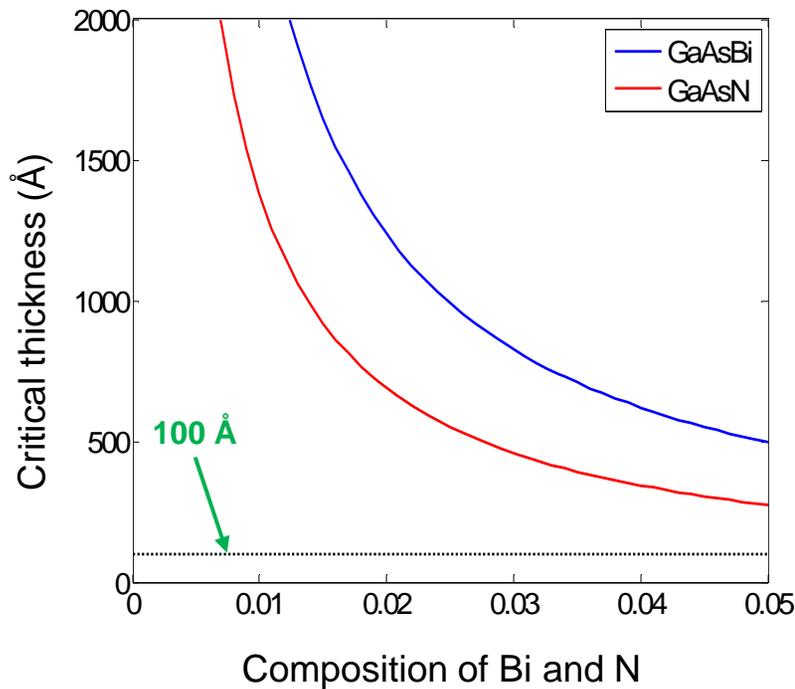
Bi (x)	N (y)
0.01	0.006
0.02	0.011
0.03	0.017
0.04	0.022
0.05	0.028

[1] N. J. Ekins-Daukes, K. Kawaguchi, and J. Zhang, Crystal Growth & Design 2, 287 (2002)



# Strain-Balanced SLS

- Critical thickness of GaAsBi and GaAsN on GaAs substrate



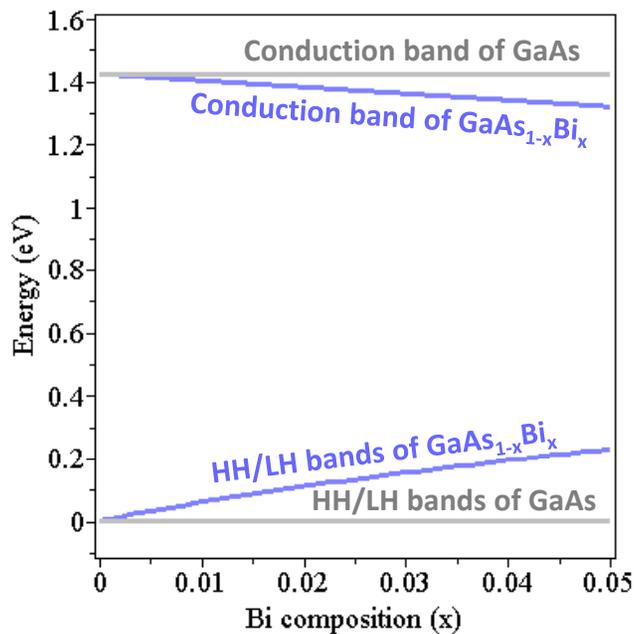
$$d_c \cong \frac{a_s}{2|\epsilon|}$$



# Band alignment – Bi, N alloys

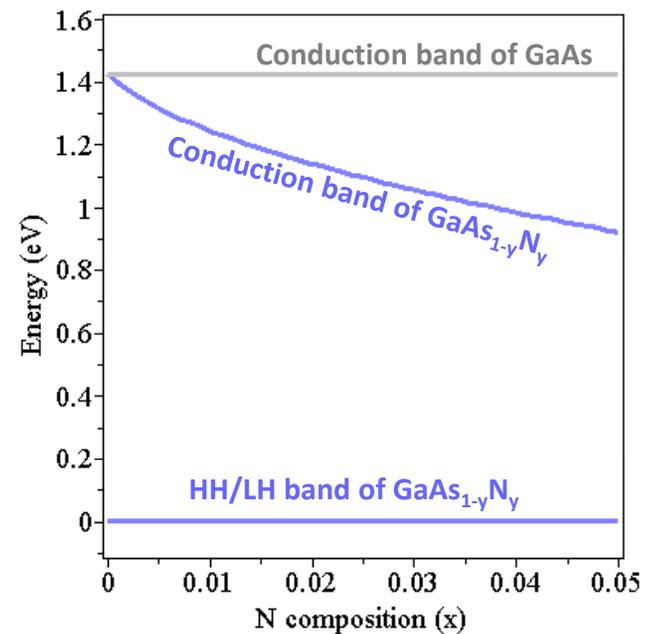
## GaAsBi

### Conduction and Valence band alignment<sup>[2]</sup>



## GaAsN

### Conduction and Valence band alignment<sup>[3]</sup>



[2] K. Alberi, J. Wu, W. Walukiewicz, K. M. Yu, O. D. Dubon, S. P. Watkins, C. X. Wang, X. Liu, Y. -J. Cho, and J. Furdyna, Phys. Rev. B. 75, 45203 (2007)

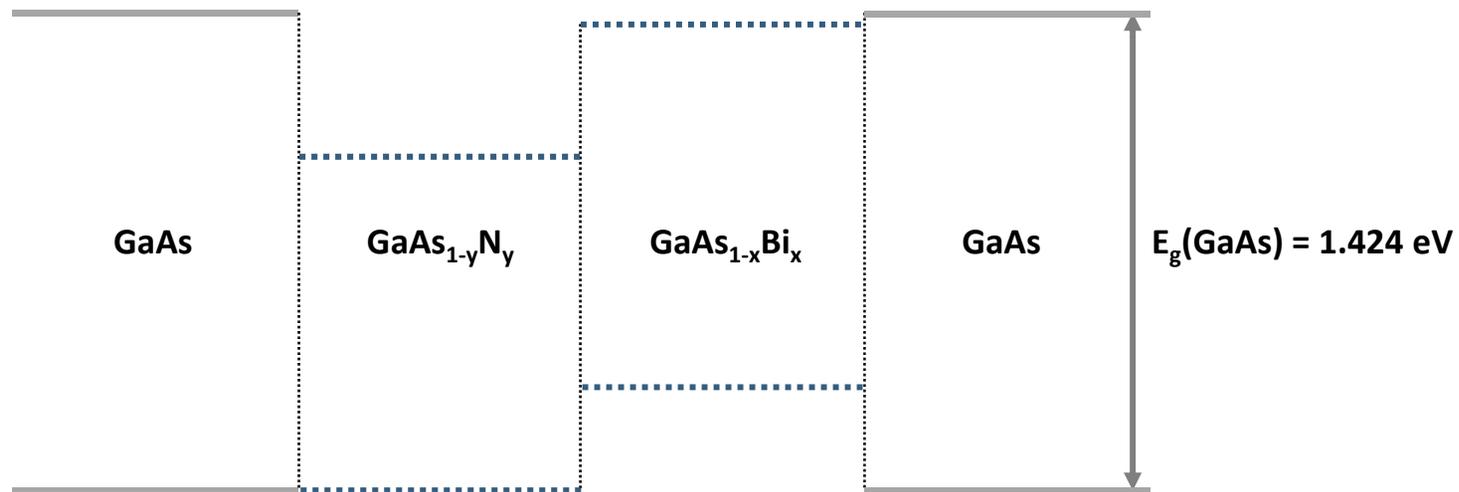
[3] W. Shan, W. Walukiewicz, K. M. Yu, J. W. Ager III, E. E. Haller, J. F. Geisz, D. J. Friedman, J. M. Olson, S. R. Kurtz, H. P. Xin, and C. W. Tu, Phys. Stat. Sol 223, 75 (2001)





# Band alignment- Bi, N Alloys

- General Band alignment of  $\text{GaAs}_{1-x}\text{Bi}_x$  ( $x=0\sim 0.05$ ),  $\text{GaAs}_{1-y}\text{N}_y$  ( $y=0\sim 0.05$ ), and GaAs





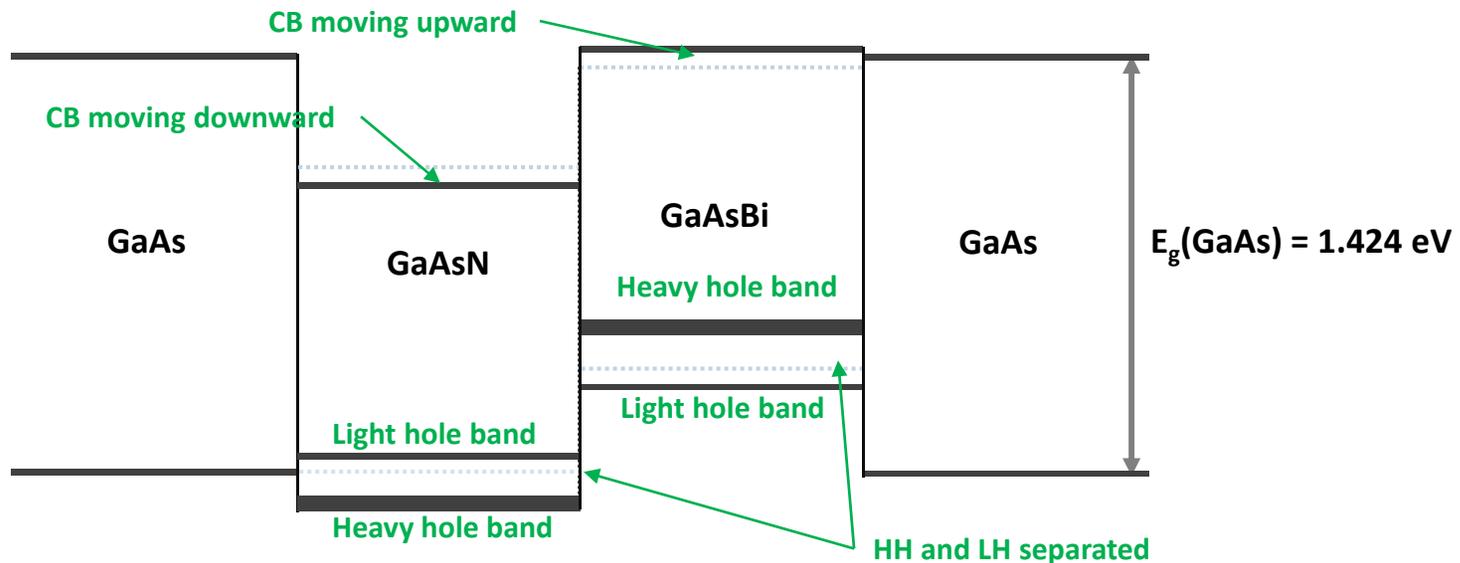
# Band alignment - Strain effect

## □ Strain effect on band alignment

- GaAsBi: Compressive strain / GaAsN: Tensile strain
- Pseudomorphically grown on a (100)-oriented substrate

$$E_{C-HH}(\mathbf{k} = \mathbf{0}) = E_g + a(\epsilon_{xx} + \epsilon_{yy} + \epsilon_{zz}) - (b/2)(\epsilon_{xx} + \epsilon_{yy} - 2\epsilon_{zz})$$

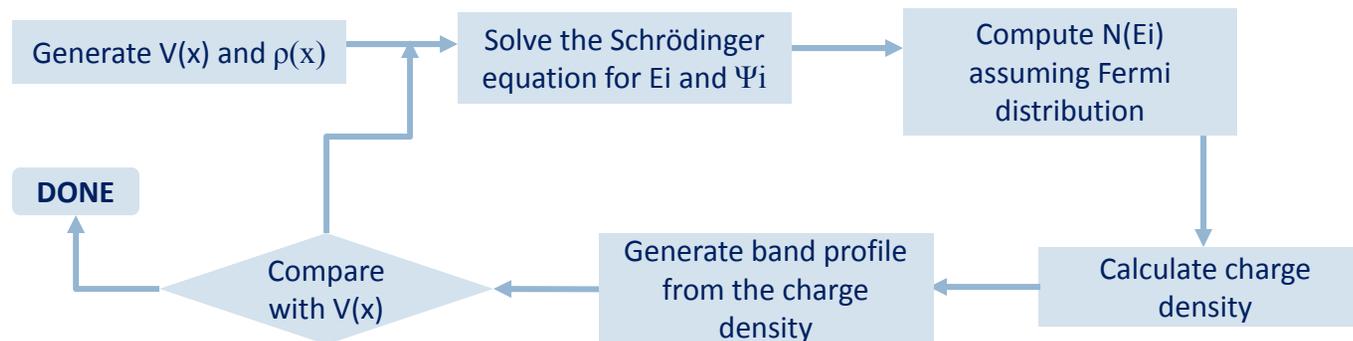
$$E_{C-LH}(\mathbf{k} = \mathbf{0}) = E_g + a(\epsilon_{xx} + \epsilon_{yy} + \epsilon_{zz}) + (b/2)(\epsilon_{xx} + \epsilon_{yy} - 2\epsilon_{zz}) \quad a = a_c - a_v$$





# Electronic Structure Calculation

## □ Coupled Schrödinger – Poisson Equation<sup>[4]</sup>



## □ Solving Schrödinger equation

- Calculate subband structure in the superlattice
- Transfer matrix approach<sup>[5]</sup> used

[4] C. H. Fischer IV, Ph.D. dissertation. University of Michigan (2004)

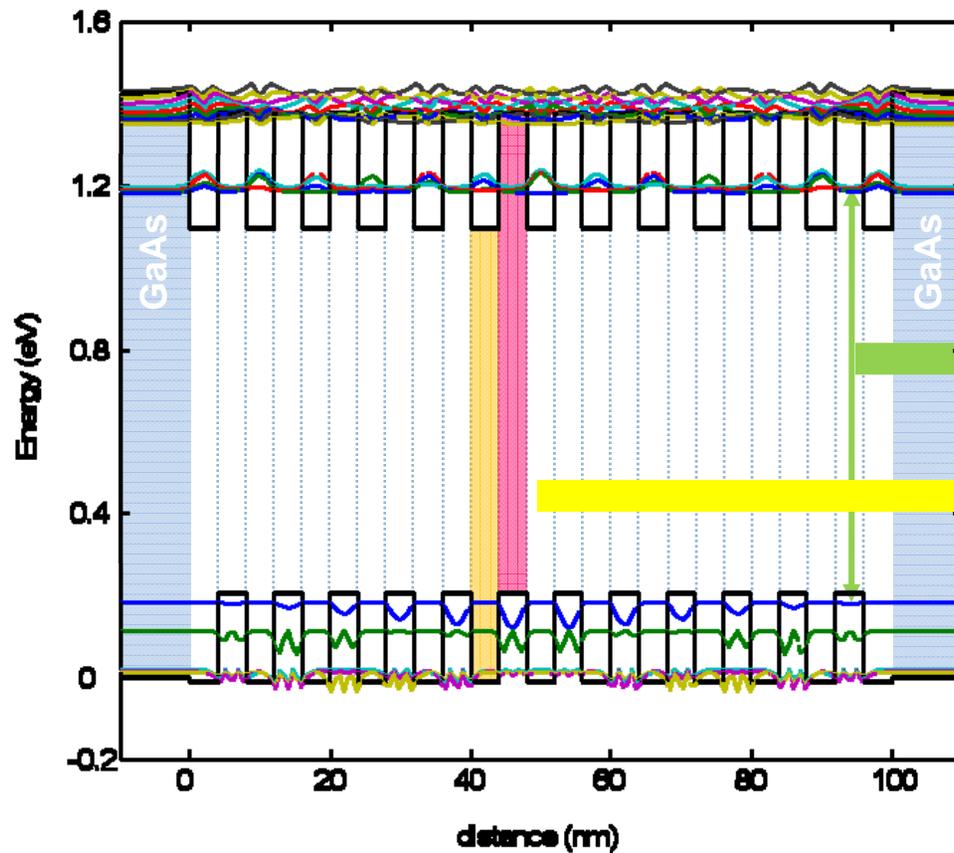
[5] E. Anemogiannis, E. N. Glytsis, and T. K. Gaylord, IEEE Journal of Quantum Electronics 29, 2731 (1993)



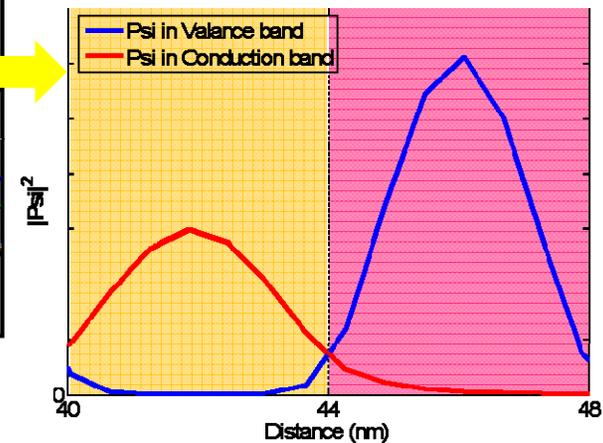


# Miniband structure of SLS

## Miniband of $\text{GaAs}_{0.96}\text{Bi}_{0.04} / \text{GaAs}_{0.979}\text{N}_{0.021}$



Layer thickness	
$\text{GaAs}_{0.96}\text{Bi}_{0.04}$	40 Å
$\text{GaAs}_{0.979}\text{N}_{0.021}$	40 Å
# of layers	25
Total thickness of SLS	100nm
Effective band gap	1.0011 eV

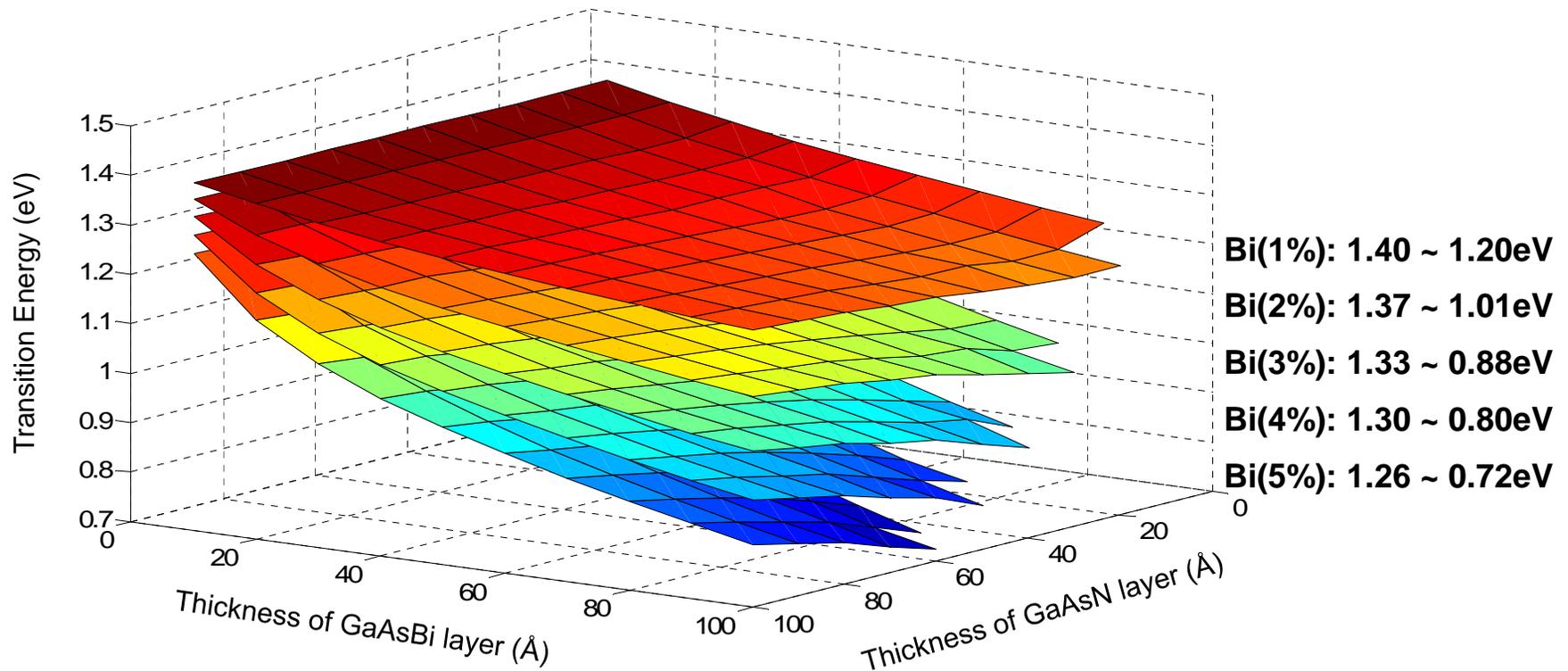




# Transition energy of SLS

## □ Transition energy range for different Bi composition

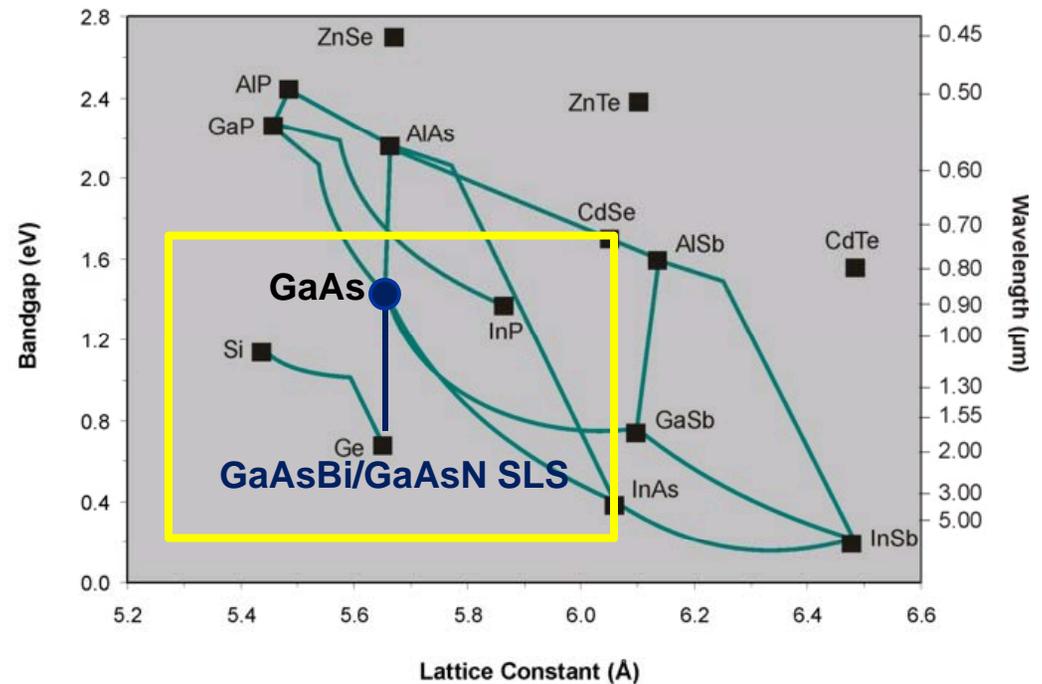
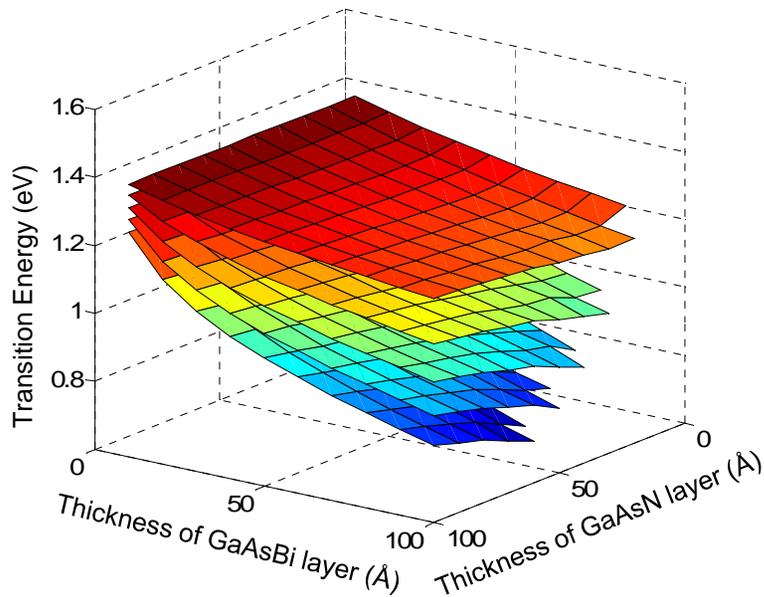
Composition of Bi and N: 0 ~ 5%





# Transition energy of SLS

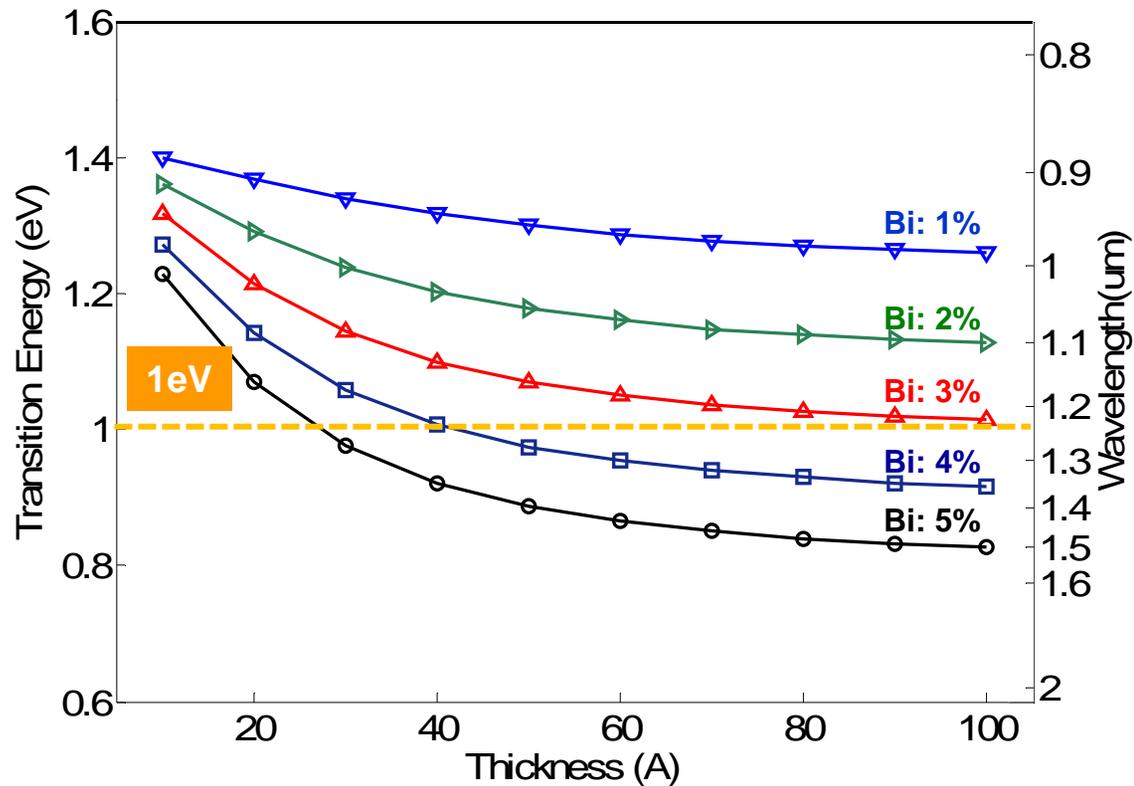
- Transition energy range for different Bi composition





# Results

- Thickness of individual layer vs. transition energy with different N and Bi composition ( $t_{1,\text{GaAsBi}} = t_{2,\text{GaAsN}}$ )





# Future work

- **Carrier transport simulation**
  - Tunneling probability
  - Carrier scattering probability via Monte-Carlo simulation
  - Determine electron transport in vertical and lateral directions
- **Radiative transitions**
  - Wavefunction overlap
  - Optical absorption/recombination lifetimes
- **Compare with experimental data**
  - Material parameters, band offsets, etc, used in simulation
  - Experimental SLS structures





# Conclusions

- **Electronic structure of GaAsBi/GaAsN superlattices were calculated for varying layer thickness and alloy composition**
- **GaAsBi/GaAsN superlattices offer a wide range of effective bandgap energy ( $\sim 0.7 - 1.4$  eV) for strain-balanced structures on GaAs**
- **Attractive for variety of optoelectronic devices, and need further experimental and theoretical research efforts**



Center for Solar & Thermal  
Energy Conversion (CSTEC)

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